

The Effect of Ca-Fe Substitution on the Clinopyroxene Crystal Structure

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Abstract

The major structural change resulting from Ca-Fe substitution in four clinopyroxenes of intermediate composition between hedenbergite and ferrosilite, measured at room temperature, is in the size and shape of the *M2* polyhedron, whereas the *M1* polyhedron remains essentially unchanged. The decrease in the average size of the *M2* polyhedron associated with a compositional change from hedenbergite to ferrosilite causes kinking of the tetrahedral chain and concomitant increases in the out-of-plane tilting of the basal face of the tetrahedron. As the *M2* polyhedron decreases further in size, the space group changes from *C2/c* to *P2₁/c* at about $\text{Fs}_{50}\text{Wo}_{50}$ composition. When the composition changes from $\text{Fs}_{50}\text{Wo}_{50}$ to $\text{Fs}_{100}\text{Wo}_0$, the *A* chain extends and finally reverses its kink direction. The anisotropic temperature factors for these intermediate compositions may be explained as a result of the effects of positional disorder.

Introduction

Most minerals can form solid solutions, either limited or complete, and thus some sites in the unit cells of minerals are occupied statistically by more than one atomic species. If there is a large difference in the ionic radii of the atoms occupying the site, the crystal structure may change with a change in occupancy of the site and thus in the apparent size of the coordination polyhedron. One of the best mineralogical examples of multiple occupancy is augite-pigeonite, where substitution of Ca for Fe or Mg is involved.

In the pyroxene quadrilateral (diopside-enstatite-ferrosilite-hedenbergite system) the clinopyroxene space groups are *P2₁/c* for Ca-poor (pigeonite) compositions and *C2/c* for Ca-rich (augite) compositions at room temperature. The major differences between

the *P2₁/c* and *C2/c* structures are that (1) there is only one crystallographically distinct silicate chain in the *C2/c* structure, whereas two types of the chains exist in the *P2₁/c* structure, and (2) the *M2* site¹ is eight-coordinated in the *C2/c* end members (diopside: Clark, Appleman, and Papike, 1969; hedenbergite: Veblen, 1969, and Cameron *et al.*, 1973) and six-coordinated in the *P2₁/c* end members (clinoferrosilite: Burnham, 1967; clinoenstatite: Morimoto, Appleman, and Evans, 1960).

In clinopyroxenes of intermediate composition, the *M2* site is very irregular as a result of multiple occupancy of the large Ca and small Fe or Mg atoms in the site. In a structural refinement of a pigeonite, $\text{Mg}_{0.35}\text{Fe}_{0.65}\text{Ca}_{0.05}\text{SiO}_3$ from Mull, Scotland, Morimoto and Güven (1970) reported a very irregular *M2* coordination polyhedron, which they concluded was an average of eight and six coordinations. Güven (1969) studied the relationship between the average size of *M2* and kinking of the

¹ Nomenclature for the pyroxenes is that proposed by Burnham *et al.* (1967).

tetrahedral chain. Takeda (1972) discussed variation of $M2-O$ bonds in clinopyroxenes as a function of Ca content and showed that the $M2$ polyhedron becomes very irregular, thus highly unstable, in the middle of the solid solution. He proposed that irregularity of the $M2$ polyhedral shape provided a structural explanation for the presence of a miscibility gap. In their crystal structural study of six end-member clinopyroxenes at high temperatures, Cameron *et al* (1973) explained the increased solid solution between the Ca-poor and Ca-rich clinopyroxenes at high temperature by the change in $M2$ coordination associated with the $P2_1/c-C2/c$ phase transition.

The present study is concerned primarily with the effects of chemical substitution on the structure studied at room temperature. To eliminate the structural effects of possible changes of Mg-Fe distribution in the cation sites, the binary join hedenbergite ($CaFeSi_2O_6$)-clinoferrrosilite ($Fe_2Si_2O_6$) was selected. Therefore, these structures reflect solely a difference between Ca and Fe contents. Furthermore, if the $M1$ site on the join studied is occupied only by Fe atoms, as expected from its polyhedral size, it is possible to isolate the effects of changes of the $M2$ site on the other parts of the structure, especially the tetrahedral chain configuration.

Experimental

Unit Cell and Space Group

Synthetic single crystals of clinopyroxenes on the hedenbergite-clinoferrrosilite join were kindly supplied by Dr. D. H. Lindsley. Synthesis techniques were described by Lindsley and Munoz (1969, Appendix). Crystals of $Fs_{85}Wo_{15}$, $Fs_{80}Wo_{20}$, $Fs_{75}Wo_{25}$

(all synthesized at 20 kbar and 950°C), and $Fs_{65}Wo_{35}$ (6 kbar and 1140°C) have been examined using the Buerger precession camera. Class b reflections ($h+k = \text{odd}$) are exhibited by $Fs_{85}Wo_{15}$ and some crystals of $Fs_{80}Wo_{20}$, whereas long-exposure photographs of $Fs_{85}Wo_{25}$, $Fs_{70}Wo_{30}$, and the other crystals of $Fs_{80}Wo_{20}$ do not show these b reflections. Thus the (metastable) boundary at room temperature between the space groups $P2_1/c$ and $C2/c$ is close to the $Fs_{80}Wo_{20}$ composition on the join hedenbergite-ferrosilite. At low pressures the clinopyroxene of this composition is not stable relative to the assemblage fayalite + tridymite (Bowen, Schairer, and Posnjak, 1933; Lindsley and Munoz, 1969). No exsolved phases are detected on long-exposure precession photographs, and thus the crystals are considered to be homogeneous.

Unit-cell parameters of crystals other than $Fs_{80}Wo_{20}$ were measured using a back-reflection precision Weissenberg camera. Data for both $CuK\alpha_1$ and $K\alpha_2$ wavelengths were refined by the least-squares method and included corrections for film shrinkage, camera eccentricity, and specimen absorption (Burnham, 1962). Unit-cell parameters for $Fs_{80}Wo_{20}$ were determined by a lattice-constant refinement subroutine for a four-circle diffractometer. This subroutine, which is a part of the Geophysical Laboratory diffractometer system, has some new features: auto-centering of reflections and least-squares refinement of the orientation matrix from which the unit-cell parameters (Table 1) are calculated (Finger, unpublished; Gabe, Alexander, and Goodman, 1970). Analysis of the clinopyroxene lattice deformation due to chemical substitution on this join is given elsewhere (Ohashi and Burnham, 1973).

Measurement and Reduction of X-Ray Intensity Data

Intensity data were collected using a computer-controlled Picker four-circle diffractometer with Nb-filtered $MoK\alpha$ radiation. Reflections in one quadrant of reciprocal space within the range 0.1 to 0.8 of $\sin \theta/\lambda$ were measured employing $\omega-2\theta$ scans. The observed intensities were corrected for Lorentz and polarization effects and for absorption using the numerical integration techniques of Burnham (1966). In addition, the secondary extinction factor of Zachariasen (1968) was calculated for the $Fs_{75}Wo_{25}$ and $Fs_{80}Wo_{20}$ crystals.

The crystal of $Fs_{85}Wo_{15}$ is twinned on (100). Therefore, the $hk0$ reflections contain superimposed contributions from both twin components. By com-

TABLE 1. Unit-Cell Parameters and Unit-Cell Volume of Ca-Fe Clinopyroxenes

	$Fs_{85}Wo_{15}$	$Fs_{75}Wo_{25}$	$Fs_{80}Wo_{20}$	$Fs_{85}Wo_{15}$
a (Å)	9.812(1)*	9.781(2)	9.760(6)	9.779(1)
b (Å)	9.049(1)	9.072(2)	9.057(8)	9.083(1)
c (Å)	5.233(1)	5.246(2)	5.234(3)	5.258(1)
β (deg.)	105.34(1)	106.55(2)	106.78(5)	107.39(1)
V (Å ³)	446.1(1)	446.2(3)	444.1(6)	445.9(2)
Method**	BW	SU	FD	BW

*Parenthesized figures represent the estimated standard deviation (esd) in terms of least units cited for the value to their immediate left, thus for 9.812(1) read 9.812 ± 0.001.

**BW: back-reflection Weissenberg camera.

FD: four-circle diffractometer.

*Compositions are in molecular proportions of Fs ($FeSiO_3$) and Wo ($CaSiO_3$). Crystals of $Fs_{85}Wo_{15}$ and $Fs_{75}Wo_{25}$ were examined using the electron microprobe. No inhomogeneities were observed with the error in composition estimated to be less than 3 mole percent Fs.

Space group
Size of crystal
Linear absorption coefficient (for $MoK\alpha$)
Range of transmission factor
Number of reflections used in refinement
Residual factor
 $\frac{\Sigma |F_o - F_c|^2}{\Sigma F_o^2}$
* $\frac{h}{a} = \frac{h'}{a'} \cos \beta$
 $\frac{g(\text{std.})}{g(\text{std.})} = \frac{h^2}{h'^2} \cos^2 \beta$

paring the several $hk0$ of one crystal made for

H1
(Fe) $\frac{h}{a}$
 $\frac{k}{b}$
 $\frac{l}{c}$
Eq.**

H2
Ca occ.
Fe occ.
 $\frac{h}{a}$
 $\frac{k}{b}$
 $\frac{l}{c}$
Eq.

S1
 $\frac{h}{a}$
 $\frac{k}{b}$
 $\frac{l}{c}$
Eq.

O1
 $\frac{h}{a}$
 $\frac{k}{b}$
 $\frac{l}{c}$
Eq.

O2
 $\frac{h}{a}$
 $\frac{k}{b}$
 $\frac{l}{c}$
Eq.

O3
 $\frac{h}{a}$
 $\frac{k}{b}$
 $\frac{l}{c}$
Eq.

*Fractional coordinates. Coord. $x, y, z \leq 1/2$
**Eq. = Equivalent temperature factor (1959).
†Parenthesized term of least 0.906(1) read
‡Occupancy of

TABLE 2. Crystal and Refinement Data for Ca-Fe Clinopyroxenes

	Fe ₆₅ Wo ₃₅	Fe ₇₅ Wo ₂₅	Fe ₈₀ Wo ₂₀	Fe ₈₅ Wo ₁₅
Space group	$C2/c$	$C2/c$	$C2/c$	$C2/c$
Size of crystal (mm)	0.13×0.20 ×0.39	0.03×0.04 ×0.21	0.09×0.11 ×0.14	0.07×0.08 ×0.29
Linear absorption coefficient (cm ⁻¹) for MoK α	56.28	60.74	63.14	64.98
Range of transmission factor (2)	31-36	78-85	57-67	60-70
Number of reflections used in refinement	967	492	797	1164
Residual factor (2)*	4.3 3.7 (std.)	5.8 5.5 (std.)	4.9 5.3 (std.)	6.2 4.2 (std.)

$$*R = \frac{\sum |F_o| - \sum |F_c|}{\sum |F_o|}$$

$$R(\text{std.}) = 1.96 \frac{\sum (|F_o| - |F_c|)^2 / \sum |F_o|^2}{\sum |F_o|}^{1/2}$$

paring the intensities of the two twin components for several hk reflections that were resolved, the volume of one component was estimated as 95.4 percent of the crystal volume, and the proper correction was made for the unresolved $hk0$ reflections.

TABLE 3. Atomic Positional Parameters and Equivalent Isotropic Temperature Factors for Ca-Fe Clinopyroxenes*

	Fe ₆₅ Wo ₃₅ ($C2/c$)	Fe ₇₅ Wo ₂₅ ($C2/c$)	Fe ₈₀ Wo ₂₀ ($C2/c$)	Fe ₈₅ Wo ₁₅ ($C2/c$)	
M1 (Fe)	0 0.9064(1) [†] 1/4 Eq.	0 0.9077(3) 1/4 Eq.	0 0.9050(1) 1/4 Eq.	0.2512(2) 0.6563(1) 0.2656(4) 0.67(1)	
M2 Ca occ. 1 [†] Fe occ.	0.7 0.3 0 0.2908(1) 1/4 Eq.	0.5 0.5 0 0.2747(3) 1/4 Eq.	0.4 0.6 0 0.2751(1) 1/4 Eq.	0.3 0.7 0.2536(3) 0.6182(1) 0.2443(5) 1.46(2)	
				A chain B chain	
S1	0.2901(1) 0.0910(1) 0.2310(1) Eq.	0.2936(2) 0.0898(2) 0.2436(4) 0.75(4)	0.2937(1) 0.0891(1) 0.2440(2) 0.65(2)	0.0641(3) 0.3387(4) 0.2369(5) 0.73(4)	0.5455(3) 0.6373(4) 0.2536(5) 0.63(4)
O1	0.1207(2) 0.0895(2) 0.1576(5) 0.63(3)	0.1207(6) 0.0893(8) 0.1517(11) 0.82(8)	0.1214(2) 0.0892(3) 0.1535(6) 0.78(6)	0.0729(6) 0.3407(10) 0.1601(12) 0.60(9)	0.3719(7) 0.8340(12) 0.1699(14) 0.95(11)
O2	0.3658(3) 0.2648(3) 0.3317(5) 1.10(4)	0.3706(7) 0.2626(7) 0.3496(16) 1.75(14)	0.3712(4) 0.2417(3) 0.3480(8) 1.53(8)	0.1182(9) 0.6968(11) 0.3623(17) 1.71(14)	0.6280(7) 0.9873(9) 0.3456(16) 0.99(12)
O3	0.3595(2) 0.0222(2) -0.0055(4) 0.70(3)	0.3520(7) 0.0255(7) -0.0043(14) 1.26(10)	0.3517(3) 0.0261(4) -0.0020(6) 1.14(5)	0.1002(7) 0.2299(10) 0.5172(14) 1.95(13)	0.6038(8) 0.7192(9) 0.4993(13) 1.13(12)

*Fractional coordinates refer to the conventional origin in those space groups. Coordinate translations between two origins are $x_2 = x_1 \pm 1/4$, $y_2 = y_1 \pm 1/4$, and $z_2 = z_1$.

[†]Eq. = Equivalent isotropic temperature factor computed from anisotropic temperature factors, B_{eq} , according to $B_{eq} = \frac{4}{3} \pi^2 \sum_{i,j} \sigma_{ij}^2 a_i^2 a_j^2$ (Hamilton, 1959).

[‡]Paranthetical figures represent the estimated standard deviation (esd) in terms of least units cited for the value to their immediate left, thus for 0.9064(1) read 0.9064 ± 0.0001.

[§]Occupancy of the M2 site is fixed by bulk chemical composition (see text).

Refinement Procedures

Throughout all refinements, the least-squares program RFINE of Finger was used on the IBM 370 and the UNIVAC 1108 computers. Atomic scattering factors were those of Fe²⁺, Ca²⁺, Si⁴⁺, and O⁻ given by Cromer and Mann (1968) with the anomalous dispersion coefficients of Cromer (1965).

Least-squares refinements of Fe₈₅Wo₃₅ and Fe₈₅Wo₁₅ were initiated with atomic parameters of hedenbergite (Veblen, 1969) and clinoferrosilite (Burnham, 1967), respectively. Refined parameters of Fe₈₅Wo₃₅ and Fe₇₅Wo₂₅, respectively, were used as initial parameters of Fe₇₅Wo₂₅ and Fe₈₀Wo₂₀. Reflections were weighted according to $w = 1/\sigma^2$, where σ is the estimated standard deviation of the observed structure factor. Reflections were rejected from least-squares refinement if the intensity was below two standard deviations of the observed intensity based on counting statistics. At the later stage of least-squares refinement, reflections with $\Delta F = F_o - F_c$ greater than 6 were also rejected.

In each structure the atomic positions, anisotropic temperature factor coefficient, and a scale factor were refined. In addition, the isotropic extinction parameter of Zachariasen (1968) was refined for the Fe₇₅Wo₂₅ and Fe₈₀Wo₂₀ data sets. The correction for the twinning in Fe₈₅Wo₁₅ was tested by refining a separate scale factor for $(hk0)$. The resulting values were essentially identical, confirming the validity of the prior correction. No strong correlations between parameters were found for the $C2/c$ structural refinements. However, the A and B chains in the $P2_1/c$ structure are in general highly correlated: -0.75 between β_{12} 's of SiA and SiB and -0.71 between β 's of O1A and O1B were found to be the strongest correlations.

From an ionic size consideration, all Ca atoms are assumed to occupy the larger M2 site. Thus, for example, the occupancy of cation sites for Fe₈₅Wo₁₅ is 100 percent Fe²⁺ in the M1 site and (70 percent Fe²⁺ + 30 percent Ca) in the M2 site.

Data for the crystals and refinements are summarized in Table 2. The final positional parameters and temperature factors are given in Tables 3 and 4, respectively. Tables of observed and calculated structure factors may be ordered.[‡]

[‡]To receive a copy of these structure factor tables, order document AM-75-001 from the Business Office, Mineralogical Society of America, suite 1000 lower level, 1909 K Street, N.W., Washington, D. C. 20006. Please remit \$1.00 for the microfiche.

TABLE 4. Anisotropic Temperature Factors for Ca-Fe Clinopyroxenes*

	Fe ₆₅ Wo ₃₅	Fe ₇₅ Wo ₂₅	Fe ₈₀ Wo ₂₀	Fe ₈₅ Wo ₁₅
M1				
F11	0.0017(1)**	0.0019(2)	0.0017(1)	0.0018(1)
F22	0.0010(1)	0.0025(2)	0.0015(1)	0.0022(1)
F33	0.0016(2)	0.0018(8)	0.0013(3)	0.0017(3)
F12	0	0	0	0.0002(2)
F13	0.0008(1)	0.0012(3)	0.0022(1)	0.0012(1)
F23	0	0	0	0.0004(4)
M2				
F11	0.0025(1)	0.0026(3)	0.0022(1)	0.0020(1)
F22	0.0074(1)	0.0100(4)	0.0105(2)	0.0082(1)
F33	0.0050(2)	0.0105(11)	0.0105(6)	0.0079(3)
F12	0	0	0	-0.0001(2)
F13	0.0001(1)	-0.0007(4)	0.0010(2)	-0.0001(1)
F23	0	0	0	0.0007(4)
			A chain	B chain
S1				
F11	0.0014(1)	0.0018(2)	0.0015(1)	0.0012(2)
F22	0.0012(1)	0.0019(2)	0.0016(1)	0.0014(2)
F33	0.0018(2)	0.0103(9)	0.0106(4)	0.0081(7)
F12	-0.0002(1)	-0.0001(3)	-0.0003(1)	-0.0007(3)
F13	0.0011(1)	0.0019(3)	0.0028(1)	0.0028(4)
F23	-0.0003(1)	-0.0000(6)	-0.0008(2)	-0.0008(5)
O1				
F11	0.0021(2)	0.0020(5)	0.0016(2)	0.0013(5)
F22	0.0018(2)	0.0023(5)	0.0025(3)	0.0021(7)
F33	0.0056(7)	0.0114(23)	0.0106(10)	0.0084(16)
F12	0.0003(2)	0.0001(7)	0.0002(2)	-0.0000(7)
F13	0.0011(3)	0.0024(9)	0.0019(5)	-0.0008(8)
F23	0.0002(4)	-0.0025(15)	0.0000(5)	0.0002(13)
O2				
F11	0.0039(2)	0.0016(7)	0.0053(3)	0.0055(8)
F22	0.0023(2)	0.0025(7)	0.0025(3)	0.0017(8)
F33	0.0135(9)	0.0355(42)	0.0287(16)	0.0232(23)
F12	-0.0013(2)	-0.0006(6)	-0.0018(3)	0.0001(8)
F13	0.0039(4)	0.0070(14)	0.0088(6)	0.0076(14)
F23	-0.0022(4)	-0.0012(15)	-0.0050(6)	-0.0005(15)
O3				
F11	0.0018(2)	0.0021(5)	0.0018(3)	0.0006(6)
F22	0.0030(2)	0.0030(7)	0.0033(4)	0.0166(12)
F33	0.0069(7)	0.0111(23)	0.0120(11)	0.0193(25)
F12	-0.0000(2)	0.0007(6)	-0.0001(3)	0.0012(6)
F13	0.0008(3)	0.0013(9)	0.0029(4)	0.0001(11)
F23	-0.0014(4)	-0.0029(13)	-0.0032(5)	0.0105(14)

*Anisotropic temperature factors, U_{ij} , are in the form of

$$U_{ij} = \frac{1}{2} (U_{11}^2 + U_{22}^2 + U_{33}^2) + 2U_{12}U_{23} - 2U_{13}U_{22}$$

**Parenthesized figures represent the estimated standard deviation (esd) in terms of least units cited for the value to their immediate left, thus for 0.0017(1) read 0.0017 ± 0.0001.

Results and Discussion

M1 and M2 Sites

Interatomic distances for the M1 and M2 sites are given in Table 5. The M1-O bond distances (Fig. 1) and the polyhedral volume (Table 5) both show essentially no change for the M1 site with Ca-Fe substitution. This observation seems to verify the assumption that all calcium is restricted to M2 on the join studied. As characterized by the quadratic elongation and the angle variance given in Table 5 (quantities proposed by Robinson, Gibbs, and Ribbe, 1971, as measures of polyhedral distortion), the M1 polyhedron deviates slightly more from an ideal octahedron on the Fe-rich side. It is, however, still much more regular than the M2 polyhedron (quadratic elongation = 1.06 and angle variance = 164° for M2 in clinoferrisilite).

The M2 site changes from eight-coordinated in hedenbergite to six-coordinated in ferrosilite. Details

of this change are one of the main points of interest in the present study. With increasing Fe content, the M2 polyhedral volume decreases and the M2-O1 and M2-O2 distances also decrease (Fig. 1), as a result of substitution of smaller Fe atoms for larger Ca atoms. On the other hand, all four M2-O3 distances increase when the composition changes from Fe₈₀Wo₂₀ to Fe₈₅Wo₁₅. In the P2₁/c region these bonds split into two groups, one increasing and the other decreasing with further Fe enrichment. In clinoferrisilite only six M2-O distances are less than 3 Å, the approximate value of the shortest oxygen-oxygen or metal-metal distance.

This change of the M2 coordination can be visualized with the aid of Figure 2. The changes of the M2-O distances occur as a consequence of a rotation of the O3A1-O3A2 and O3B1-O3B2 vectors in

TABLE 5. Interatomic Distances M1-O and M2-O in Ca-Fe Clinopyroxenes

	Fe ₆₅ Wo ₃₅	Fe ₇₅ Wo ₂₅	Fe ₈₀ Wo ₂₀	Fe ₈₅ Wo ₁₅
M1 Site				
1 M1-O1A	2.127(2)*	2.103(6)	2.113(3)	2.116(7)
2 M1-O1B				2.103(8)
3 -O1A	2.175(2)	2.192(7)	2.187(3)	2.225(8)
4 -O1B				2.176(9)
5 -O2A	2.086(2)	2.101(7)	2.096(3)	2.109(9)
6 -O2B				2.110(8)
Mean	2.129	2.132	2.132	2.140
Quad. Elong.**	1.0042	1.0057	1.0053	1.0065
Ang. Var. (deg. ²)**	13.5	17.7	16.9	20.4
Polyhedral Volume (Å ³)	12.8	12.8	12.8	12.9
M2 Site				
1 M2-O1A	2.302(2)	2.168(6)	2.197(3)	2.179(8)
2 M2-O1B				2.161(9)
3 -O2A	2.259(3)	2.127(8)	2.133(4)	2.135(10)
4 -O2B				2.033(9)
5 -O3A1	2.765(2)	2.844(8)	2.852(4)	2.800(9)
6 -O3B2				2.859(8)
7 -O3A2	2.700(2)	2.822(7)	2.817(4)	3.058(8)
8 -O3B1				2.825(7)
Mean of 4, Nbr†	2.281	2.163	2.165	2.127
Mean of 4, Br†	2.733	2.833	2.830	2.891
Mean of 8	2.507	2.498	2.497	2.509
Polyhedral Volume (Å ³)	25.7	24.7	24.7	24.8 [8-coord.] 18.1 [7-coord.]

*Parenthesized figures represent the estimated standard deviation (esd) in terms of least units cited for the value to their immediate left, thus for 2.127(2) read 2.127 ± 0.002.

**Octahedral quadratic elongation (Robinson et al., 1971) defined by

$$\frac{\sum_{i=1}^6 (d_i/d_0)^2}{6}, \text{ where } d_0 \text{ is the center-to-vertex distance for an ideal } \frac{1}{2} \text{ octahedron whose volume is equal to that of the observed } \frac{1}{2} \text{ octahedron.}$$

$$\text{Octahedral angle variance defined by } \sum_{i=1}^{12} (\theta_i - 90)^\circ / 11.$$

†Nbr†: nonbridging oxygen atoms (O1 and O2) and

Br†: bridging oxygen atoms (O3).

Bond Distance (Å)

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2.

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FIG. 1

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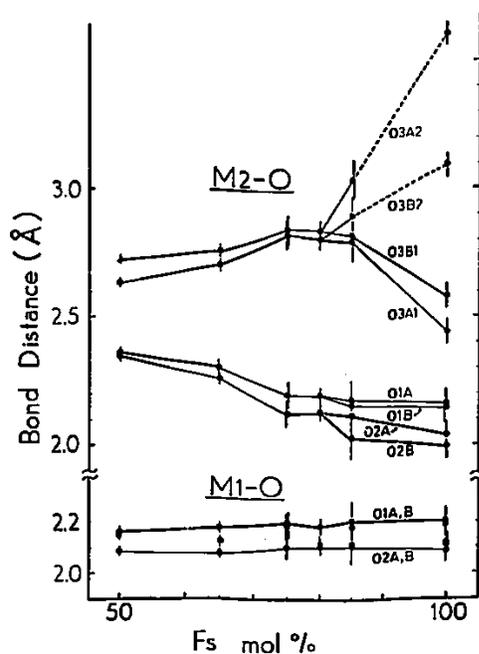


FIG. 1. Variation of $M1-O$ and $M2-O$ interatomic distances with ferrosilite content in Ca-Fe clinopyroxenes. Error bars represent ± 1 standard deviation. Data for hedenbergite and clinoferrosilite are after Cameron *et al* (1973) and Burnham (1967), respectively. See Figure 2 for details of $M2$ coordination geometry.

(100) accompanied by relative movements of the O1 and O2 atoms toward $M2$. Rotations of the $O3B1-O3B2$ vector, for example, result in an increase of $M2-O3B2$ and decrease of $M2-O3B1$.

The question arises whether the structural changes described above are real changes of polyhedral geometry. If the shape of any given $M2$ coordination polyhedron is governed only by the species of atom (Ca or Fe) occupying that site (case 1), there will be only two possible types of $M2$ polyhedra in the pyroxenes studied, one found in hedenbergite and the other in clinoferrosilite, and the crystal structure of an intermediate phase obtained by X-ray diffraction would be an average of the two. In case 1, therefore, discussion of the $M2$ polyhedral geometry for intermediate compositions would have little physical meaning because the average would not represent the real structure. On the other hand, if the shape of any given $M2$ polyhedron is determined not only by the atomic species in the site but also by those in the

neighboring $M2$ sites (case 2), then there are various possibilities for the $M2$ polyhedral shapes. In this case structural refinement of the X-ray data would still yield an average structure, but it would approximate the true structure more closely than in case 1.

Results of a Mössbauer study on these clinopyroxenes (Dowty and Lindsley, 1973) may help to resolve these two cases. The quadrupole splitting can be correlated with the degree of polyhedral distortion and thus it reflects primarily a short-range atomic arrangement around the iron atom. The change of the $M2$ quadrupole splitting (Fig. 3) indicates that the local configuration around the ferrous ion changes as the bulk chemical composition changes. Thus the $M2$ polyhedron occupied by the ferrous ion is also affected by the $Fe/(Fe + Ca)$ ratio in the rest of the structure. Therefore, it is concluded that the $M2$ polyhedron obtained from X-ray refinement is not an artifact but represents the most probable polyhedral geometry for a given chemical composition.

Both the X-ray and the Mössbauer results indicate that a great change in the $M2$ polyhedral shape occurs at compositions between $Fe_{88}Wo_{12}$ and $Fe_{100}Wo_0$ (Fig. 3). The fact that the most rapid change occurs near the Fe-rich end of the solid solution is explained by the more severe effect expected for substitution of large Ca atoms into the small $M2$ polyhedron.

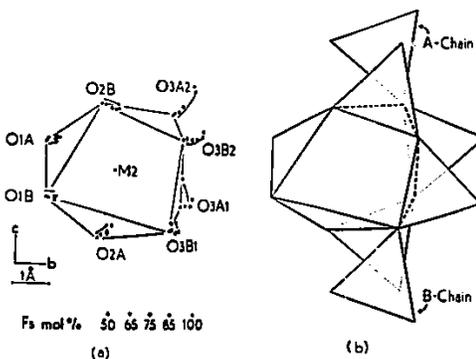


FIG. 2. (a) Variation of the oxygen positions around the $M2$ site in Ca-Fe clinopyroxenes. Arrows indicate shifts of the oxygen atoms relative to the $M2$ atom with Ca-Fe substitution; these may not represent actual shifts in the structure (see text, section on temperature factors, for discussion). Data for hedenbergite and clinoferrosilite are after Cameron *et al* (1973) and Burnham (1967), respectively. (b) Relation between the $M2$ site and the tetrahedral chains in $Fe_{88}Wo_{12}$. Note that positional changes of the O3 atoms shown in (a) result in rotations of the tetrahedral chains.

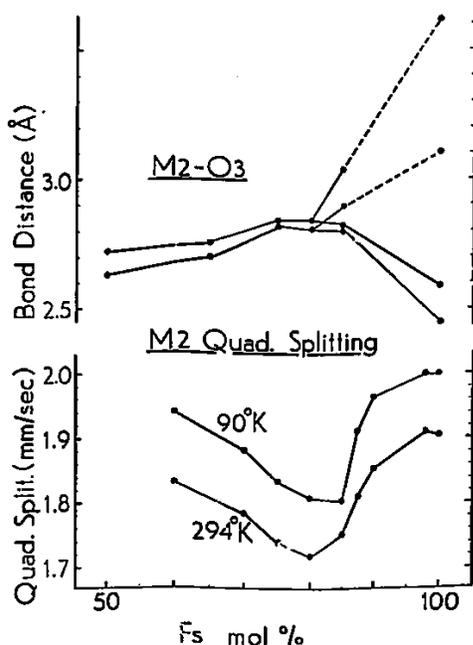


FIG. 3. Comparison of variations of the $M2$ quadrupole splitting (Dowty and Lindsley, 1973) and the $M2-O3$ interatomic distances with ferrosilite content in Ca-Fe clinopyroxenes. See Figure 1 for $M2-O1$ and $M2-O2$ distance variations. Note that both X-ray and Mössbauer studies indicate a sharp change in $M2$ polyhedral shape between the compositions $Fe_{50}Wo_{50}$ and $Fe_{100}Wo_0$.

Silicate Chains

Octahedral expansion affects the tetrahedral chains in three ways: (1) The silicate tetrahedra distort, (2) the tetrahedral chain angles change, and (3) the degree of out-of-plane tilting of the basal faces of the tetrahedra vary (Cameron *et al.*, 1973). Details of these changes associated with Ca-Fe substitution are discussed below.

Tetrahedron. Interatomic distances and angles for the silicate tetrahedra are given in Table 6. The Si-O3 (bridging oxygen) bond is the longest of the Si-O bonds, and of the two nonbridging oxygens, the Si-O2 distance is shorter than the Si-O1. The angle O1-Si-O2, $114^\circ-119^\circ$, is larger than the ideal tetrahedral angle, 109.46° .

The Si-O3 (bridging) bond distances (Fig. 4) decrease with replacement of Fe for Ca on the augite (Ca-rich) side, whereas the Si-O (nonbridging) bond distances increase. Variation on the pigeonite (Ca-

poor) side, however, is not simple because there are two crystallographically distinct silicate chains. As the composition changes from $Fe_{50}Wo_{50}$ to $Fe_{75}Wo_{25}$, expansions of the Si-O1 and Si-O2 bonds are accompanied by contractions of $M2-O1$ and $M2-O2$, respectively. For the O3 atoms, contractions of the Si-O3 bonds are coupled with expansions of the $M2-O3$ bonds. The $M1-O$ distances remain essentially constant with composition.

Qualitative discussions on bond distances can be developed by introducing a *bond strength*, defined by Zachariasen (1963). He assumes (1) that the bond strength is empirically related to the bond distance and (2) that the sum of bond strengths for each atom is set to its valence. Coupled changes in the Si-O and $M2-O$ bond distances for the same oxygen atom are a natural consequence of the constant sum of the bond

TABLE 6. Interatomic Distances and Angles for Si Tetrahedra in Ca-Fe Clinopyroxenes

	$Fe_{50}Wo_{50}$		$Fe_{75}Wo_{25}$		$Fe_{100}Wo_0$	
	A Chain		B Chain		C Chain	
Distances (Å)						
Si-O1	1.602(2)*	1.621(6)	1.614(3)	1.616(7)	1.620(7)	1.616(8)
Si-O2	1.593(2)	1.601(7)	1.596(3)	1.589(11)	1.589(11)	1.616(8)
Si-O3(1)	1.672(2)	1.657(7)	1.660(3)	1.662(8)	1.677(8)	1.677(8)
Si-O3(2)	1.657(2)	1.667(7)	1.667(3)	1.630(7)	1.640(6)	1.640(6)
Mean, Mn***	1.598	1.611	1.605	1.603	1.618	1.618
Mean, Mn**	1.665	1.662	1.654	1.636	1.659	1.659
Mean of 4	1.631	1.637	1.629	1.619	1.638	1.638
Quad. Elong****	1.0048	1.0064	1.0062	1.0016	1.0067	1.0067
O1-O2	2.728(3)	2.767(7)	2.737(4)	2.694(9)	2.755(9)	2.755(9)
O1-O3(1)	2.678(3)	2.671(8)	2.668(5)	2.643(10)	2.672(11)	2.672(11)
O1-O3(2)	2.669(3)	2.681(9)	2.639(6)	2.630(9)	2.666(9)	2.666(9)
O2-O3(1)	2.580(3)	2.574(9)	2.573(5)	2.601(10)	2.565(12)	2.565(12)
O2-O3(2)	2.655(3)	2.678(10)	2.648(5)	2.630(11)	2.652(10)	2.652(10)
O3(1)-O3(2)	2.64(1)	2.644(2)	2.639(2)	2.654(2)	2.688(2)	2.688(2)
Angles (deg.)						
O1-Si-O2	117.2(1)	117.0(4)	117.0(2)	116.4(6)	118.7(6)	118.7(6)
O1-Si-O3(1)	109.7(1)	109.2(3)	109.2(2)	108.4(4)	108.3(4)	108.3(4)
O1-Si-O3(2)	109.9(1)	109.2(3)	109.2(2)	108.2(4)	109.7(6)	109.7(6)
O2-Si-O3(1)	106.4(1)	106.4(6)	106.4(2)	107.3(5)	107.2(5)	107.2(5)
O2-Si-O3(2)	109.5(1)	110.0(6)	109.6(2)	109.9(4)	109.1(6)	109.1(6)
O3(1)-Si-O3(2)	105.3(1)	106.6(2)	107.1(1)	108.4(3)	108.2(3)	108.2(3)
Ang. Var. (deg. ²)	20.7	18.4	17.9	6.9	26.2	26.2
O3-O3-O3**	162.5(2)	159.8(5)	159.5(3)	164.2(8)	156.0(7)	156.0(7)
Si-O3-Si	136.5(1)	136.6(5)	136.8(2)	140.9(3)	135.5(5)	135.5(5)
Out-of-plane tilting***						
	3.7	4.5	4.7	4.2	5.8	5.8
Tetrahedral Volume (Å³)						
	2.214	2.233	2.206	2.175	2.236	2.236

*Parenthesized figures represent the estimated standard deviation (esd) in terms of least units cited for the value to their immediate left, thus for 1.602(2) read 1.602 ± 0.002 .

**nbr = nonbridging oxygen atoms (O1 and O2), and

br = bridging oxygen atom (O3).

***Tetrahedral quadratic elongation (Robinson *et al.*, 1971) defined by

$\sum_{i=1}^4 (\frac{d_i}{d_0})^2 / 4$, where d_0 is the center-to-vertex distance for an ideal tetrahedron whose volume is equal to the observed tetrahedron.

****Tetrahedral angle variance (Robinson *et al.*, 1971) defined by

$\sum_{i=1}^6 (\theta_i - 109.47)^2 / 6$.

*****Tetrahedral chain angle. All chains listed here are O rotation (Thompson, 1970).

*****Angle between (100) and the basal face, O2-O3-O3, of a tetrahedron.

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strengths. When the strength of one bond increases, that of another must decrease to maintain the sum constant. Because only three cations are coordinated to the O2 atom, the bond strengths for Si-O2, M1-O2, and M2-O2 are larger (thus shorter in length) than any other corresponding bonds for the O1 and O3 oxygens.

Tetrahedral Chain Angle. The tetrahedral chain angle, O3-O3-O3, has been shown to vary with chemical composition, particularly with Ca content, and also with temperature (Clark *et al.*, 1969; Brown *et al.*, 1972; Smyth and Burnham, 1972; Cameron *et al.*, 1973). Proper attention must be given, however, not only to angles but also to the rotation direction with respect to the octahedra (Thompson, 1970; Papike *et al.*, 1973). Overlooking the difference in the rotation sense, the chain in augites is often compared with the A chain in pigeonites on the basis of the apparent similarity of the tetrahedral chain angle, which is 165° for hedenbergite (Cameron *et al.*, 1973) and 167° for the A chain in clinoferrosilite (Burnham, 1967). The sense of rotation is, however, reversed in these chains.

The variation of the tetrahedral chain angles with composition is plotted in Figure 5. As the effective size of M2 decreases by substitution of Fe for Ca, the

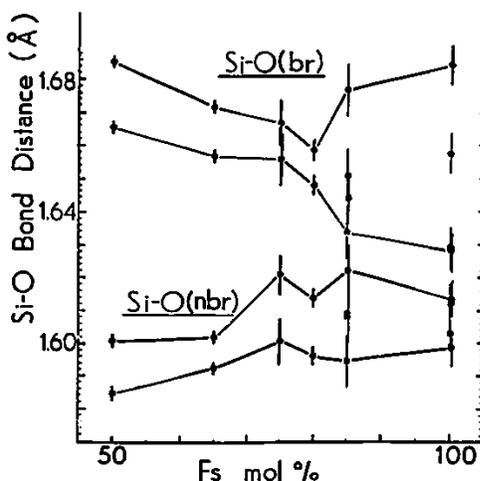


FIG. 4. Variation of Si-O interatomic distances with ferrosilite content in Ca-Fe clinopyroxenes. Error bars represent ± 1 standard deviation. O(br) denotes the bridging oxygen atoms, O3; O(nbr) denotes the nonbridging oxygen atoms, O1 and O2. Distances in hedenbergite and clinoferrosilite are after Cameron *et al.* (1973) and Burnham (1967), respectively.

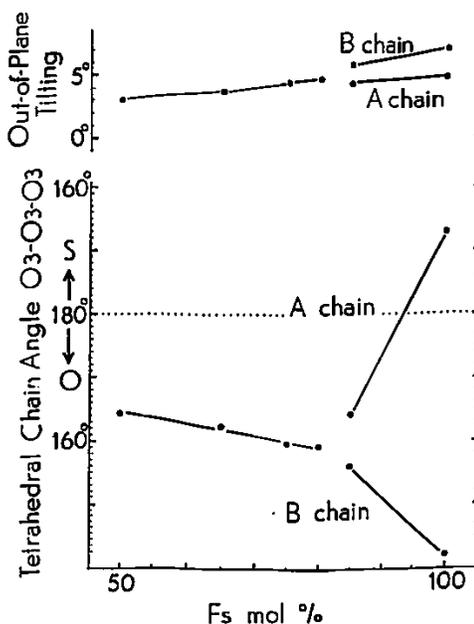


FIG. 5. Variation of the tetrahedral chain angle, O3-O3-O3, and the out-of-plane tilting of the basal triangle, defined by O2, O3, and O3, with the ferrosilite component in Ca-Fe clinopyroxenes. Angles for hedenbergite and clinoferrosilite were computed from the atomic coordinates given by Cameron *et al.* (1973) and Burnham (1967), respectively. Standard errors are smaller than the radii of circles.

chain becomes more kinked, from 165° in $\text{Fs}_{50}\text{Wo}_{50}$ to 159° in $\text{Fs}_{50}\text{Wo}_{20}$. The relation between the M2 site and the tetrahedral chains can be visualized using Figure 2: a vector connecting O3B1 and O3B2 can be seen to rotate clockwise when the composition changes from $\text{Fs}_{50}\text{Wo}_{50}$ to $\text{Fs}_{50}\text{Wo}_{20}$, and this rotation results in a decrease in the O3-O3-O3 angle. As the size of M2 decreases further from $\text{Fs}_{50}\text{Wo}_{20}$, the chains on opposite sides of each M2 polyhedron become crystallographically distinct. The B chain becomes increasingly kinked, whereas the A chain becomes extended and reverses its rotation direction between $\text{Fs}_{85}\text{Wo}_{15}$ and $\text{Fs}_{100}\text{Wo}_0$. Thus in $\text{Fs}_{100}\text{Wo}_0$ the A chain is "S-rotated" (Thompson, 1970) and the B chain is "O-rotated."

Out-of-Plane Tilting of the Basal Face of the Tetrahedron. The out-of-plane tilting of the basal face of the tetrahedron, which is defined as the angle between (100) and the basal face,

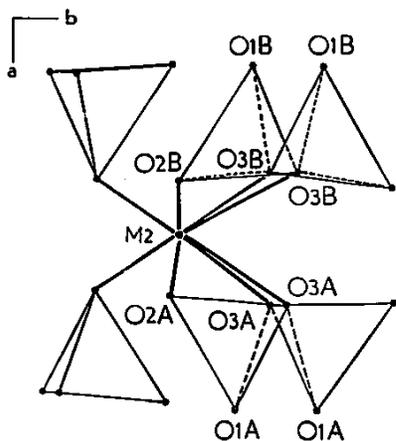


FIG. 6. A portion of the $Fs_{100}Wo_0$ structure showing the relation between the $M2$ site and the out-of-plane tilting of the basal face of the tetrahedron. The $O2$ atoms shift slightly toward $M2$ and away from the (100) plane, passing through the $O3$ atoms. As a result, the basal face of the tetrahedron tilts a few degrees with respect to (100) . Out-of-plane tilting increases when the effective ionic size of $M2$ decreases, as would be expected from shortening of $M2-O2$ bonds.

$O2-O3-O3'$, of the tetrahedron, provides another measure to describe the silicate tetrahedral chain configuration. The direction of the observed tilting is such that the $O1$ and $O2$ atoms in the same tetrahedron are on opposite sides of the (100) plane containing the $O3$ atoms (Fig. 6). As exhibited in Figure 5 and Table 5, the out-of-plane tilting generally tends to increase when the composition changes from hedenbergite to ferrosillite. This increased tilting is a direct response of the tetrahedral chain to the changes in the $M2$ polyhedron. When the composition changes from $Fs_{50}Wo_{50}$ to $Fs_{90}Wo_{10}$ (Fig. 1), the $M2-O2$ distances decrease but $M2-O3$ distances increase. These changes in the $M2-O$ distances will result in an increase in the out-of-plane tilting angle (Fig. 6). In the pigeonite region the tilting is larger for the B chain than for the A chain, reflecting the fact that $M2-O2B < M2-O2A$ and $M2-O3B1 > M2-O3A1$ (Fig. 1).

There is a correlation between the tilting and the tetrahedral B chain angle (Fig. 5)—the more kinked the chain angle, the greater the out-of-plane tilting. This relationship may be explained by simple geometrical arguments. The kinking of the chain results in an increase in the offset of $O3$ atom pairs parallel to b (Fig. 2b). However, these changes have

very little effect on the $O1-O1$ distance, which varies only from 3.088 Å in $Fs_{50}Wo_{50}$ to 3.040 Å in $Fs_{100}Wo_0$ as the chain angle decreases from 164.5° to 142°; therefore, the relative position of $O1$ is very nearly fixed. The only means of kinking the chain without moving $O1$ results in the movement of the $O2$ atom in such a manner that the out-of-plane tilting increases (Fig. 6).

Temperature Factors

The variation of isotropic temperature factors with composition (Fig. 7) falls into two groups: one ($M2$, $O2$, and $O3$) has a marked peak in the middle of the solid solution, whereas the other ($M1$, Si , and $O1$) is relatively flat. These differences in behavior can be explained by the effects of positional disorder due to multiple occupancy of the $M2$ site. Because the ionic radii of the Ca and Fe atoms are considerably

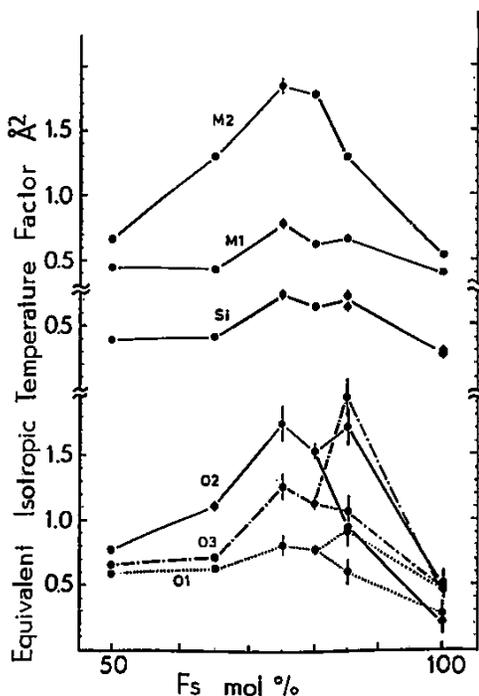


FIG. 7. Variation of equivalent isotropic temperature factors with ferrosilic content in Ca-Fe clinopyroxenes. Error bars represent ± 1 standard deviation (if not shown, the standard deviation is smaller than the radii of circles). Data for hedenbergite and clinoferrosillite are after Cameron *et al.* (1973) and Burnham (1967), respectively.

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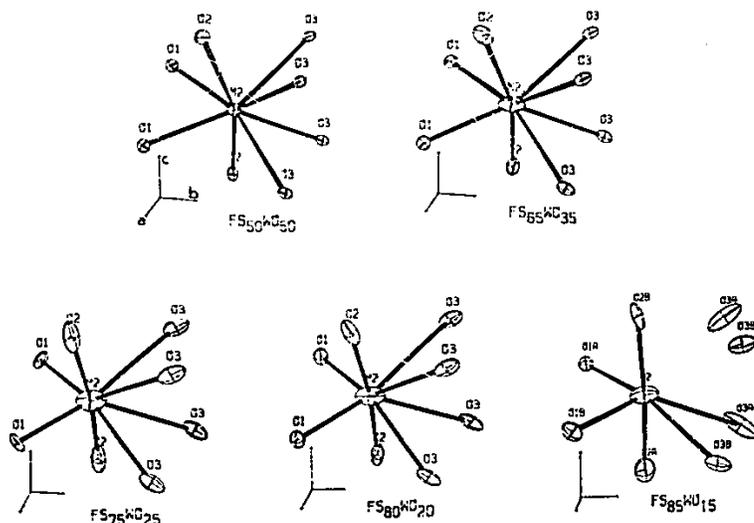


FIG. 8. Apparent thermal vibration ellipsoids for atoms in the $M2$ polyhedron in Ca-Fe clinopyroxenes. The ellipsoids represent 70 percent probability surfaces (1.92 times the r.m.s. amplitude). Ellipsoids for hedenbergite were calculated from data given by Veblen (1969). For the $O2B$ site in $Fe_{85}Wo_{15}$, β_{13} is decreased by 2 standard deviations to obtain a positive definite tensor. Drawing produced by ORTEP (Johnson, 1965).

primarily intrinsic vibrations, whereas those in intermediate compositions include significant effects of positional disorder. As for the $M2$ displacement, this study suggests the same interpretation reached by Takeda (1972). Since $O1$ shows relatively small changes in ellipsoid shape throughout the solid solution, it seems reasonable to conclude that as the composition becomes more iron-rich, the mean position

of $M2$ shifts toward $O1$ rather than the other way.

In intermediate compositions the longest ellipsoid axis for the $O2$ atom tends to orient parallel to the bond direction of $M2-O2$ (Fig. 9a). Since $M2-O2$ is the shortest bond in the $M2$ polyhedron, the multiple occupancy of the Ca and Fe atoms in $M2$ may produce significant disorder of $O2$ along the bond direction.

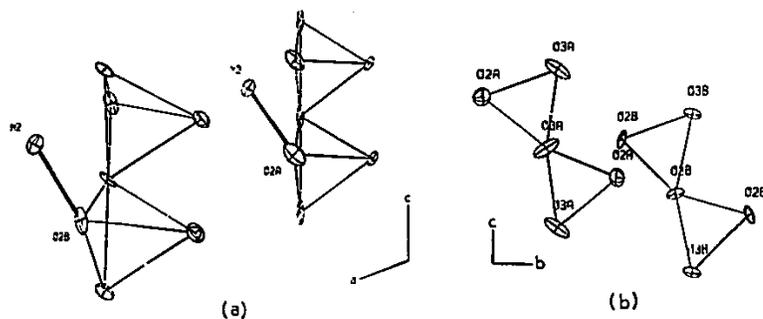


FIG. 9. Explanation of the abnormally large apparent thermal vibration ellipsoids for $O2$ and $O3$ atoms in $Fe_{85}Wo_{15}$. See text. Ellipsoids shown are 70 percent probability surfaces (1.92 times the r.m.s. amplitude). For the $O2B$ atom, β_{13} is decreased by 2 standard deviations to obtain a positive definite tensor. Drawing produced by ORTEP (Johnson, 1965).

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The large apparent thermal vibration ellipsoid for the O3 atoms in the intermediate compositions can be interpreted as positional disorder associated with tetrahedral chain rotation (Fig. 9b). As previously shown (Fig. 2) the change in size of the M2 cation causes a rotation of the tetrahedral chains. The rotation angle of the individual chains may be slightly different from the average chain angle, and the resulting positional fluctuation will appear as large apparent vibrations of O3 in (100), the approximate plane of the rotation, and along a bisecting direction of the basal faces of the two tetrahedra bridged by O3. O1 and Si, however, are close to the rotation axis and thus are not affected by this rotation.

Conclusions

As composition changes on the hedenbergite-ferrosilite join, the polyhedral volume and bond distances of the M1 site do not change appreciably, except for a slight distortion of the polyhedron. Such lack of change in M1 confirms that few, if any, Ca atoms can occupy M1 sites in the Ca-Fe clinopyroxenes studied.

In the M2 coordination polyhedron the M2-O1 and M2-O2 distances and the polyhedral volume decrease when the composition changes from hedenbergite to ferrosilite. The M2-O3 distances exhibit a sharp change between the compositions $\text{Fs}_{85}\text{Wo}_{15}$ and $\text{Fs}_{100}\text{Wo}_0$.

The decrease in the average size of the M2 atom causes kinking of the tetrahedral B chain. Extension and reversal of rotation sense of the A chain occur between the compositions $\text{Fs}_{85}\text{Wo}_{15}$ and $\text{Fs}_{100}\text{Wo}_0$. The decrease in M2 cation size causes an increase in the out-of-plane tilting of the basal face of the tetrahedron.

The large temperature factors found for the M2, O2, and O3 atoms in intermediate compositions of the Ca-Fe clinopyroxenes can be explained by the effect of atomic positional disorder due to multiple occupancy in M2.

Together with the crystal structures of the end-member clinopyroxenes at high temperatures (Cameron *et al.*, 1973), the results of the present study could provide a basis for future studies of the crystal structures of intermediate clinopyroxenes at high temperature. These studies, which will undoubtedly have mineralogical significance for a better understanding of crystallization and exsolution in natural pyroxenes, are also necessary for relating the crystal structures to the experimentally determined phase diagram.

Acknowledgments

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ORBS	CALC	H OBS	CALC	H OBS	CALC	H OBS	CALC								
14 755	747	7 256	258	14 133	132	15 72	65	12 184	182	7 1056	1090	A 129	135		
10 422	624	9 174	166	12 248	242	13 41	32			5 406	404				
8 1009	1046	11 217	194	10 41	31	11 159	157			3 1070	1027				
6 1274	1337			8 82	77	9 183	194			1 378	375				
4 533	627			4 333	321	7 103	86			1 793	778				
2 741	662			2 250	232	5 241	234			3 856	855				
0 0	4952			4 813	799	3 295	257			5 324	323				
2 744	662			2 505	511	1 76	81			7 750	744				
4 538	627			8 144	130	1 36	55			9 141	122				
6 1405	1337			10 154	143	5 157	154								
8 1437	1046					7 41	34								
10 851	824					9 199	193								
14 787	747					11 90	91								

(2)

14 747	732			14 87	84										
12 128	107			12 531	547										
10 478	971			10 102	111										
8 604	594			8 829	834										
6 1386	1435			6 371	376										
4 1458	1602			4 356	369										
2 106	138			2 813	799										
2 1372	1421			2 328	336										
4 1402	1476			2 491	911										
6 300	291			6 500	506										
8 677	667			8 467	461										
12 121	110														

MOORE BUSINESS FORMS, INC. PATENT PENDING

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H	ORS	CALC	H	ORS	CALC	H	ORS	CALC	H	ORS	CALC	H	ORS	CALC	H	ORS	CALC	H	ORS	CALC	
0	0	5000	-9	365*	40	-15	385	406	-13	442	425	-7	260	275	-11	197	218	-5	409	404	
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4	530*	592				-9	998	1004	-9	296	300	-3	263	250	-5	331	308	1	194*	256	
6	1425	1381	H 1 A			-5	1088	1112	-7	1101	1118	-1	169	176	-3	207	153	5	426	453	
8	972	1017				-3	658	653	-5	351	331	3	259	274	-1	657	652				
10	870	898	-9	250*	141	-1	1467*	1532	-3	1159	1132	5	315	317	3	169	112	H 13	3		
14	632	662	-3	444*	365	1	852	896	-1	447	427	7	176	130	5	604	603				
						3	237	228	1	887	876				9	188	199	-5	429	424	
H 0 2			H 2 0			5	1181	1127	3	1284	1319				H 7 3			-1	276	278	
						7	421	427	7	708	697							1	234	277	
						9	629	642	9	343	361	-9	343	362							
-14	671	682	0	193	211				11	514	499	-5	454	444	-7	211*	133				
-10	946	949	2	790	774							-1	432	441	-3	182	171				
-8	575	561	4	250	261	H 3 4						1	191	187				0	214	179	
-6	1485	1489	8	312	316				9	192*	108	-9	181	211							
-4	1635	1646										5	478	465							
0	1904*	2037	H 2 1									9	235	208							
2	1448	1467				H 3 5			-9	265	247										
4	1475	1471	-12	753	774				-7	239	242	H 7 4				-9	328	313			
6	445	409	-8	618	606	-13	266*	47	-3	405	378				-5	399	389	-4	238	235	
8	517	517	-6	593	579	-11	318	280	-1	252	269	-9	231*	164	-1	362	365	-2	408	427	
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			-2	184*	1734	-7	330	307	7	272*	205	-1	174	158							
H 0 4			0	151	184	-5	638*	730				5	237	192							
			2	1394	1394	-3	200	157	H 5 4												
-14	728	720	4	691	682	-1	894*	974							0	608	615				
-12	339	322	6	727	725	1	641	668	-13	598	588				4	424	439				
-10	697	652	8	625	650	3	206	227	-11	272	307	-11	278*	200	6	259	253				
-8	220	219	12	576	576	5	677	649	-7	912	901	-5	473	456	10	395	404				
-6	1101*	1241				7	233	242	-5	345	327	-1	235	224							
-4	872*	1148				9	538	509	-3	855	859	1	251	263							
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2	513	504	-10	267	271	H 3 7			1	566	588				-2	246	239				
4	471	1012	-8	192	207	-11	233	212	3	608	773				0	244	290				
6	539	578	-6	150	498	-9	380	323	5	203	208	-3	232	233							
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			4	151	131	3	223	277							-6	292	279				
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			-6	226	228				-3	741	783	H A 1									
-A	239*	0	-4	407	415	-12	418	437	-1	234	202				-12	573	579				
			-2	1430*	1519	-10	212	183	3	532	500	-10	107	193	-10	386*	323				
H 0 8			0	218	252	-8	153	153	5	220	220	-8	611	600	-6	307	302				
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-8	279*	203	4	283	279	-2	521	518	H 6 0			-4	526	532	0	431	419				
-4	530*	279	6	636	619	0	548	541	0	1694	1726	-2	1276	1288	4	349	331				
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						12	222	234	6	505	517	8	409	413	H 10 5						
H 1 0									8	429	463	12	601	604	-4	183*	107				
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			8	182	157	2	377	369				-12	509	574							
H 1 1						4	173	147	H 6 2			-8	607	583	1	440	428				
												-6	209	309	3	466	482				
-11	165	144	H 2 5									-4	422	377	7	600	645				
-7	285	283										-2	940	902	9	213	190				
-5	182	181	-12	448	436	H 4 3			-14	574	573										
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7	267*	324	-2	554*	678	-8	424	408	-6	974	993	4	162	165							
			0	218	239	-4	196	155	-4	494*	593	6	479	474	-3	195	201				
H 1 2			-2	674	724	-2	726	754	-2	175	200	8	546	558							
			6	321	309	0	274	275	0	1405	1419										
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-4	194*	24				6	180	208	4	602	607	H A 4				-7	662	655			
-7	1231	1221	H 2 6			12	251*	191	6	289	299				-3	486	458				
-3	267*	334							8	301	303	-12	199	169	-1	168	164				
-1	418	459	-2	220	202	H 4 4			10	630	621				1	387	426				

H	ORS	CALC	H	ORS	CALC	H	ORS	CALC	H	ORS	CALC	H	ORS	CALC	H	ORS	CALC			
H 6 2			H 7 1			H A 0			H A 6			H 9 6			H 11 1			H 12 3		
-8 361 394			-13 71 64			0 50 34			-10 76 71			-7 111 91			-9 156 129			-8 173 157		
-7 123 114			-11 140 140			5 65 60			-9 89 70			-3 91 87			-7 116 118			-6 79 82		
-6 1044 1063			-10 72* 8			8 189 182			-8 138 126			H 10 0			-3 293 262			-4 93 69		
-5 70 66			-9 164 162			8 286 283			-4 80 71						-1 184 159			-2 219 189		
-4 725 731			-7 80 77			12 130 122			-3 73 36						3 205 184			-2 154 132		
-3 93 94			-5 605 627						-2 193 216			-10 338 348			5 183 159			4 95 80		
-2 134 136			-3 154 154			H A 1			-2 92 101			-8 73 62			7 133 116					
0 1443* 1510			-1 174 188									-6 198 220						H 12 4		
1 63 48			1 424 449			-13 115 71			H A 7			-4 335 359			H 11 2			-6 262 231		
2 616 639			5 317 314			-12 572 583			0 499 522			0 499 522						-4 385 339		
3 98 98			7 74 49			-11 57 53			4 340 359			-10 75 67						-2 100 116		
4 629 637			9 296 294			-10 206 187			6 189 220			-9 140 136						0 267 231		
6 403 404						-9 72 37			8 68 62			-7 680 666						2 116 82		
8 326 324			H 7 2			-8 573 613			10 344 348			-6 82 37								
10 729 716						-6 323 327						-5 166 159								
12 105 91			-13 80 79			-5 95 94			H 9 0			-4 75 60						H 13 0		
			-9 94 95			-8 551 556						-3 493 482								
H 6 3			-7 270 288			-2 1245 1270			H 10 1			-1 221 210						-7 87 64		
			-5 332 342			2 735 746			-10 173 188			0 83 62						-5 195 195		
-12 129 134			-3 253 263			4 604 610			-8 122 126			1 439 436						-1 117 111		
-10 91 77			-1 121 118			6 624 620			-7 67 67			3 677 663						1 102 111		
-6 89 83			1 104 87			8 465 461			-6 135 129			5 66 34						5 197 195		
-3 54 74			3 276 294			11 82* 15			-4 177 180			7 413 411						7 71 64		
-2 74 70			5 332 329						-2 217 216											
0 122 107			7 164 164			H A 2			0 336 337			2 80 72			H 11 3			H 13 1		
2 156 167			9 60 59						2 80 72			4 106 91								
4 81 83						-12 141 152			4 106 91			6 73 57						-5 358 378		
6 64 52			H 7 3			-8 214 212			8 68* 66			8 68* 66						-3 84 98		
10 71 44						-6 280 199			10 197 181			10 197 181						-1 288 303		
			-11 97 95			-4 143 127												1 224 243		
H 6 4			-9 298 286			-2 241 237			H 10 2									5 391 401		
			-7 80 73			-1 51 9														
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-12 191 174			-2 64 24			1 56 42			-1 421 404			-8 105 107						-5 189 201		
-11 69 84			-1 294 320			2 333 341			1 364 341			-6 229 236						-3 73 61		
-10 595 603			0 67 37			4 150 137			3 188 167			-4 296 302						-2 90 53		
-8 73 64			1 126 141			6 93 71			5 806 800			0 484 504						-1 133 108		
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-6 641 646			5 418 415			10 99 89			11 218 208			6 213 212								
-5 87 76			7 91 84									8 74 47								
-4 418 435			9 127 119			H A 3														
-3 123 120						-12 564 577			H 10 3											
-2 95 109			H 7 4			-10 237 228														
-1 66 53						-9 122 88			-11 82 76			-10 176 174						-5 382 382		
0 626* 693			-13 163 155			-8 598 594			-7 130 114			-4 86 84						-1 222 247		
2 302 332			-9 180 176			-6 342 328			-5 58 38			-2 103 96						1 237 251		
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4 755 780			-7 282 286			-4 371 379			1 56 44			1 70 50						H 14 0		
6 351 344			-5 183 178			-3 55 50			3 80 88			2 126 135						-4 77 46		
7 75 34			-3 134 149			-2 934 944			5 72 48			4 130 129						-2 168 118		
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